

Characterizing wildfire regimes in the United States

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Wildfires statistics for the conterminous United States (U.S.) are examined in a spatially and temporally explicit manner. We use a high-resolution data set consisting of 88,916 U.S. Department of Agriculture Forest Service wildfires over the time period 1970–2000 and consider wildfire occurrence as a function of ecoregion (land units classified by climate, vegetation, and topography), ignition source (anthropogenic vs. lightning), and decade. For the conterminous U.S., we (i) find that wildfires exhibit robust frequency–area power-law behavior in 18 different ecoregions; (ii) use normalized power-law exponents to compare the scaling of wildfire-burned areas between ecoregions, finding a systematic change from east to west; (iii) find that wildfires in the eastern third of the U.S. have higher power-law exponents for anthropogenic vs. lightning ignition sources; and (iv) calculate recurrence intervals for wildfires of a given burned area or larger for each ecoregion, allowing for the classification of wildfire regimes for probabilistic hazard estimation in the same vein as is now used for earthquakes.

frequency–area statistics | power-law distribution | Bailey ecoregion divisions | U.S. Department of Agriculture Forest Service | probabilistic hazard

Over the last decade, high-profile wildfires (1, 2) have resulted in numerous fatalities and loss of infrastructure. Wildfires also have a significant impact on climate and ecosystems; recently, several researchers (3–7) have emphasized the need for regional-level examinations of wildfire-regime dynamics and change, and the factors driving them. With implications for hazard management, climate studies, and ecosystem research, there is, therefore, significant interest in appropriate analysis of historical wildfire databases. Insightful studies using wildfire database statistics exist (5–24) but are often hampered by the low spatial and/or temporal resolution of their data sets. Here, we use a high-resolution database of wildfires for the conterminous United States (U.S.), combined with techniques drawn from recent advances in statistical physics and complexity theory, to examine U.S. wildfire statistics in a spatially and temporally explicit manner.

Statistical physics and complexity theory have begun to be applied to a wide range of natural hazards (e.g., refs. 25 and 26). One characteristic of many of these studies is power-law (scale-invariant) statistical distributions (27), in which the probability of a certain value occurring is raised to some power of that value. For instance, earthquakes follow a power-law relationship of the frequency (number) vs. energy released, the Gutenberg–Richter relationship (28). The frequency–size statistics of many other natural hazards also appear to satisfy power-law distributions to a good approximation under a wide variety of conditions (29). These natural hazards include asteroid impacts (30, 31), landslides (32, 33), volcanic eruptions (34), and the subject of this paper, wildfires. Power-laws and other “heavy-tailed” distributions are increasingly being used by reinsurance companies and governments for probabilistic hazard analysis (35, 36) and are playing a growing role in environmental and social policy decisions.

The wildfire regime encompasses the timing, frequency, and magnitude of all wildfires that occur in a region. The term “wildfire,” as used in this paper, is taken to mean any burned

area, irrespective of size or ignition source. Recent studies of wildfire regimes suggest frequency–area probability distributions that are power-law (8–13) or otherwise “heavy-tailed” (14–19) over many orders of wildfire area. The power-law takes the form

$$f(A_F) = \alpha A_F^{-\beta}, \quad [1]$$

with frequency density $f(A_F)$, the number of wildfires in “unit” bins with A_F burned area, and β and α constants. Local and broad regional studies of wildfires in the U.S. (9), Australia (9), Italy (10), and China (12), for example, have shown power-law behavior with exponents ranging from $\beta = 1.1$ –1.8, over two to five orders of magnitude of wildfire area, for 120–9,000 individual wildfire events. However, the low spatial and temporal resolution of the data sets used in these studies has made analyses as a function of wildfire regime drivers difficult. Therefore, in this paper, we use a high-resolution data set (discussed in the next section) consisting of U.S. Department of Agriculture Forest Service (USFS) wildfire-occurrence records [ref. 37; the wildfire data discussed in ref. 37 were obtained through personal communication with T. J. Brown (University of Nevada, Reno)] for $N_{FT} = 88,916$ wildfires ($A_F \geq 0.004 \text{ km}^2 = 1 \text{ acre}$) between 1970 and 2000. We then examine the resultant wildfire burned-area statistics both spatially and temporally at regional scales as a function of ecological and anthropogenic driving factors. First, we will discuss the data and methods; next, the results of analyses; and, finally, the general implications of having robust power-law behavior for wildfire statistics in each ecoregion.

Data and Methods

Data Quality and Completeness. Using 657,949 wildfires recorded between 1970 and 2000 by the USFS and the U.S. Department of the Interior (DOI), Brown *et al.* (37) compiled an inventory and performed a coarse assessment of the quality of historical federal wildland wildfire-occurrence records. They found 90.7% (324,122 wildfires) of USFS records and 71.0% (214,687 wildfires) of the DOI records “useable” in terms of their completeness and spatial coordinates. Furthermore, they note that DOI wildfire reporting was not continuous for most of the 1970s and that for both the USFS and DOI data, counts of very small wildfire sizes are often incomplete because wildfires may go undetected or unreported. Therefore, in our study we use only those Brown *et al.* (37) records (i) from the USFS and (ii) with areas $A_F \geq 0.004 \text{ km}^2 = 1 \text{ acre}$, giving in our data set (for 1970–2000) a total number of wildfires $N_{FT} = 88,916$ and total area burned $A_{FT} = 68,994 \text{ km}^2$ (see Table 1 for numbers of wildfires and area burned per ecoregion). Wildfires in our study were classified as “anthropogenic” (64% by number) or “lightning” (36%) according to the description given by Brown *et al.* (37). All nonanthropogenic fires are here termed “lightning,” because of the very small occurrence (<0.01%) of “other” natural causes (e.g., volcanism) (37).

Abbreviations: U.S., United States; USFS, U.S. Department of Agriculture Forest Service.

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Table 1. Results by Bailey ecoregion divisions in the conterminous U.S. for frequency–area and recurrence-interval analyses of USFS wildfires

Ecoregion division name	Ecoregion division code	Ecoregion division area, km ²	USFS area, km ²	A _{FT} , km ²	N _{FT}	β	logα	r ²	T (≥0.01 km ²), T (≥10 km ²), yr	
									yr	yr
Hot Continental	[220]	969,955	32,068	1,132.4	8,429	1.75 ± 0.11	−3.81 ± 0.12	0.974	0.19 ± 0.10	34 ± 20
Hot Continental Mtns.	[M220]	192,955	43,609	815.4	7,353	1.75 ± 0.09	−4.05 ± 0.10	0.984	0.30 ± 0.14	55 ± 27
Marine	[240]	38,591	1,147	8.0	58	1.37 ± 0.21	−3.99 ± 0.31	0.972	0.89 ± 0.69	23 ± 22
Marine Mtns.	[M240]	138,300	67,360	2,813.5	3,875	1.53 ± 0.05	−4.36 ± 0.07	0.989	2.47 ± 0.73	100 ± 37
Mediterranean	[260]	88,319	2,546	2,918.6	475	1.30 ± 0.05	−3.44 ± 0.07	0.987	0.22 ± 0.05	2 ± 1
Mediterranean Mtns.	[M260]	241,388	99,798	16,055.4	11,882	1.46 ± 0.05	−3.93 ± 0.06	0.989	0.51 ± 0.13	13 ± 4
Prairie	[250]	772,597	1,583	39.4	316	1.48 ± 0.15	−3.60 ± 0.19	0.964	0.28 ± 0.19	9 ± 8
Savanna	[410]	20,202	0	0	0					
Subtropical	[230]	1,064,749	42,920	2,670.2	16,423	1.81 ± 0.07	−3.74 ± 0.09	0.987	0.12 ± 0.05	33 ± 14
Subtropical Mtns.	[M230]	22,792	6,667	142.0	1,816	1.70 ± 0.12	−3.82 ± 0.15	0.974	0.24 ± 0.15	32 ± 21
Temperate Desert	[340]	689,458	39,210	3,890.7	2,391	1.39 ± 0.05	−4.09 ± 0.07	0.985	0.85 ± 0.22	13 ± 5
Temperate Desert Mtns.	[M340]	112,924	27,289	1,027.9	885	1.39 ± 0.07	−4.38 ± 0.08	0.984	1.66 ± 0.54	27 ± 13
Temperate Steppe	[330]	1,099,973	43,841	3,034.5	2,466	1.46 ± 0.05	−4.18 ± 0.06	0.990	0.89 ± 0.23	22 ± 8
Temperate Steppe Mtns.	[M330]	585,081	300,383	26,281.0	15,487	1.49 ± 0.04	−4.34 ± 0.06	0.993	1.18 ± 0.26	36 ± 10
Tropical/Subtropical Desert	[320]	447,811	13,306	1,658.4	2,379	1.47 ± 0.07	−3.69 ± 0.08	0.984	0.29 ± 0.09	8 ± 3
Tropical/Subtropical Steppe	[310]	657,342	28,536	2,179.6	4,138	1.57 ± 0.06	−3.95 ± 0.07	0.990	0.40 ± 0.12	20 ± 7
Tropical/Subtropical Steppe Mtns.	[M310]	130,018	42,861	3,949.3	8,594	1.54 ± 0.06	−3.93 ± 0.07	0.989	0.41 ± 0.12	18 ± 6
Warm Continental	[210]	381,507	47,453	374.4	1,888	1.69 ± 0.08	−4.71 ± 0.10	0.988	1.70 ± 0.76	203 ± 99
Warm Continental Mtns.	[M210]	112,924	5,983	2.9	61	1.68 ± 0.28	−5.18 ± 0.41	0.988	13.64 ± 12.88	1,672 ± 1616
Totals		7,766,886	846,560	68,993.6	88,916					

Given for each Bailey ecoregion division (38) (Fig. 1A) in the conterminous U.S. are the following: division name; division code (M = mountain areas); area of division; area of USFS lands within the ecoregion division (Fig. 1B); the total area, A_{FT}, and total number, N_{FT}, of wildfires occurring in USFS lands (1970–2000) irrespective of ignition source and included in the data set used for analyses in this paper (ref. 37; and see *Data and Methods*); and the results of frequency–area and recurrence-interval analyses. Frequency–area parameters β and logα are from Eq. 1, $f(A_F) = \alpha A_F^{-\beta}$, where in each case the best fit was estimated for $\log[f(A_F)] = -\beta \log[A_F] + \log \alpha$, with coefficient of determination r² as given. Error bars on β and logα are ±2σ (standard deviations) and approximately equivalent to upper/lower 95% confidence intervals. Error bars were obtained from each variable's standard error and degrees of freedom based on the number of 'bins' used in the least-squares fit. For completeness, all fits are shown; however, care should be taken in interpreting β and logα based on small data samples (e.g., N_{FT} < 100). Recurrence intervals T(≥A_F) are obtained from Eq. 5 and represent the average time between wildfires ≥0.01 km² and ≥10 km², occurring in spatial areas of 1,000 km² within each ecoregion. Associated error bars again represent ±2σ (standard deviations) or 95% confidence intervals, calculated for each ecoregion by using the upper/lower 95% confidence interval values as given in this table for β and logα.

Bailey's Ecoregions. To allow spatial analyses with regard to the biophysical factors that drive wildfire regimes, we classify the USFS wildfire data into the ecoregion divisions developed by Bailey (38) (Fig. 1A). Ecoregions distinguish geographic regions that share common biophysical characteristics. In Bailey's classification (38), a three-level hierarchy is used: domains (based primarily on climate), divisions (climate, vegetation, and soils), and provinces (climate, vegetation, soils, land-surface form, and fauna). Mountainous areas within specific divisions and provinces are also classified. In the conterminous U.S., there are three domains, subdivided into 19 divisions and further divided into 34 provinces. Ecoregion divisions are shown in Fig. 1A, with division names, codes, and areas in Table 1. Using Bailey's ecoregion division level in our analyses allows spatial disaggregation of the data, at a resolution suitable for the study of potential wildfire-regime drivers, while ensuring that an adequate number of wildfires are available for statistical analyses. Wildfires occurring on USFS lands are used as a representative sample of the ecoregion division in which they are located. USFS land area per ecoregion is given in Table 1, with the spatial distribution in the conterminous U.S. shown in Fig. 1B. Of the 18 ecoregion divisions with wildfire data, USFS lands range from 0.2% (Prairie) to 51.3% (Temperate Steppe Mtns.) of the respective ecoregion's area.

Frequency–Area Statistics. In each ecoregion division, we examine the frequency–area statistics of USFS wildfires. Because the wildfire inventories used are not “complete” (there are many more “smaller” wildfires than measured), probability densities are not appropriate; instead, we use frequency densities $f(A_F)$ defined as

$$f(A_F) = \frac{\delta N_F}{\delta A_F}, \quad [2]$$

where A_F is the wildfire burned area and δN_F is the number of wildfires in a “bin” of width δA_F. The frequency densities $f(A_F)$ are then the number of wildfires per “unit” bin. We use frequency densities because cumulative frequencies can obscure underlying trends in finite data sets (39). Because there are many more small wildfires than larger ones, we increase our bin width δA_F with increasing area A_F, to give approximately equal bin widths in logarithmic coordinates. The USFS areas over which the wildfires occur change from one ecoregion to another (Table 1 and Fig. 1B). Therefore, to allow specific comparison between ecoregions, we take the frequency densities $f(A_F)$ (fires·km^{−2}) and normalize them by (i) the USFS area (km²) within each ecoregion and (ii) the period of observation (yr), to give normalized frequency densities $f(A_F)$ (fires·yr^{−1}·km^{−4}).

For each ecoregion division, the normalized frequency densities $f(A_F)$ are plotted as a function of wildfire area A_F. As we will show later (see *Results*), an excellent fit in each case is given by the inverse power-law distribution (Eq. 1), a two-parameter distribution that forms a straight line in log–log space. In each case, we estimate the best fit for $\log[f(A_F)] = -\beta \log[A_F] + \log \alpha$, where β is the gradient and logα is the y-intercept. The power-law exponent β quantifies the ratio of the number of large to small wildfires in a given area, with β = 0 indicating the same number of large as small wildfires (per “unit” size bins). As β increases, large events become rarer with respect to small ones. The y-intercept, or logα, is the normalized number of wildfires per unit bin; in our case, A_F = 1 km².

Calculation of Recurrence Intervals. An extension of having the two parameters α and β in the inverse power-law distribution given

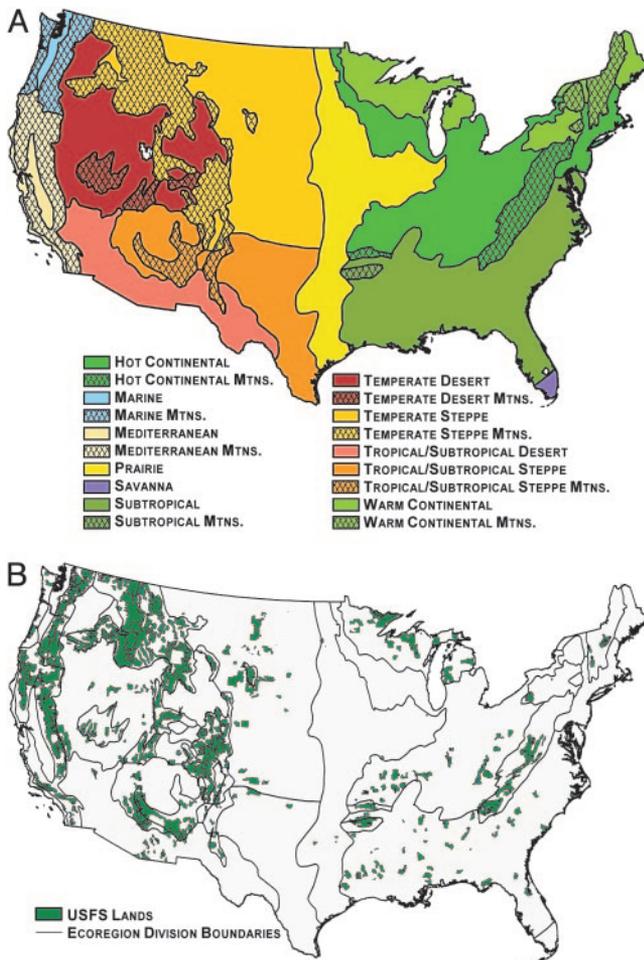


Fig. 1. Bailey's ecoregion divisions and USFS lands. (A) In Bailey's classification (38), the conterminous U.S. is divided into ecoregion divisions according to common characteristics of climate, vegetation, and soils. Mountainous areas within specific divisions are also classified. In this paper, we use ecoregion divisions to geographically subdivide an extensive database of wildfire-burned areas for statistical analyses as a function of ecoregion division. (B) Location of USFS lands in the conterminous U.S. Table 1 gives each ecoregion division area and the total area of USFS lands within each ecoregion.

in Eq. 1 is the calculation of the recurrence interval $T(\geq A_F)$, based on the probability that in a defined spatial area (i.e., some specific region A_R), a given size event with area A_F will be equaled or exceeded in any given year. For example, if in a defined region there is an average 1 in 100 chance per year that a wildfire of area ≥ 10 km² will occur, this size event (10 km²) is said to have a 100-yr recurrence interval. In other words, assuming that the events are uncorrelated in time (Poissonian), then for this region there will be, on average, 100 yr between wildfires of size 10 km² or greater. In calculating the recurrence intervals associated with different wildfire areas A_F , we first take the integral of Eq. 1 to arrive at $N_{CF}(\geq A_F)$, the cumulative number of wildfires with areas greater than or equal to A_F , giving (for $\beta > 1$)

$$N_{CF}(\geq A_F) = \int_{A_F}^{\infty} f(A'_F) dA'_F = \tau A_R \left(\frac{\alpha}{\beta - 1} \right) A_F^{1-\beta}, \quad [3]$$

where α and β are constants from Eq. 1, τ is the data set duration in years, and A_R is the spatial area over which the probabilistic

“hazard” is to be considered. As A_R increases, the number of wildfires of a given size or larger $N_{CF}(\geq A_F)$ in that region also increases. We could terminate the integral in Eq. 3 at some A_{max} instead of infinity, because the power-law distribution given in Eq. 1 must have some upper bound. However, because the numbers of the most extreme events are few, the shape of the tail at these extreme values is unclear. Therefore, we choose to consider “small” and “medium” values of A_F , well below the maximum wildfire area that might occur in any given ecoregion.

Using a Weibull equation, the recurrence interval $T(\geq A_F)$ associated with a wildfire of a given area or larger is $\tau + 1$, the total number of years in the data set plus one, divided by $N_{CF}(\geq A_F)$, giving (for $\beta > 1$)

$$T(\geq A_F) = \frac{\tau + 1}{N_{CF}(\geq A_F)} = \left(\frac{\tau + 1}{\tau} \right) \left(\frac{\beta - 1}{\alpha} \right) \left(\frac{A_F^{\beta-1}}{A_R} \right). \quad [4]$$

The length of our data set is $\tau = 31$ yr, and we consider the recurrence interval of wildfires in spatial areas of $A_R = 1,000$ km², giving (for $\beta > 1$)

$$T(\geq A_F) = 1.032 \times 10^{-3} \text{ km}^2 \left(\frac{\beta - 1}{\alpha} \right) A_F^{\beta-1}, \quad [5]$$

with A_F in km² and $T(\geq A_F)$ in years. In *Results*, we present recurrence intervals by ecoregion for $A_F = 0.01$ km² and $A_F = 10$ km² for spatial areas within each ecoregion of $A_R = 1,000$ km².

Results

Frequency–Area Statistics of Wildfires. In Table 1, for each ecoregion division, we give the results of our normalized frequency–area analyses. Each ecoregion division exhibits excellent frequency–area power-law behavior ($r^2 \geq 0.96$) over more than five orders of magnitude for burned area. In each case, the wildfire statistics have been examined as a function of ecoregion division, regardless of ignition source (lightning vs. anthropogenic). Also included in Table 1 are $\pm 2\sigma$ error bars (see legend) equivalent to lower/upper 95% confidence intervals for both β and $\log \alpha$. Two example analyses are given in Fig. 2, with the Mediterranean Ecoregion ($\beta = 1.30 \pm 0.05$) and the Subtropical Ecoregion ($\beta = 1.81 \pm 0.07$) exhibiting the smallest and largest β values for the 18 ecoregions, respectively. Note that care should be taken in interpreting parameter values for ecoregion divisions with very small wildfire numbers (e.g., $N_{FT} < 100$; Marine and Warm Continental Mtns.), because these have increased uncertainty in estimates for β and $\log \alpha$.

Spatial Distribution of β . We next map the spatial distribution of β values by ecoregion (Fig. 3A), where β is the result of each frequency–area analysis shown in Table 1. Fig. 3A suggests an east-to-west gradient of higher-to-lower β values across the conterminous U.S. We note that Fig. 3A does not take into account the $\pm 2\sigma$ error bars on β (95% confidence intervals) as given in Table 1. However, even taking the error bars into account, there is still strong evidence of the east-to-west gradient of β values across the conterminous U.S.

Lightning vs. Anthropogenic Wildfires. To explore alternative hypotheses given for the east-to-west gradient of β , we examine wildfire records with reference to ignition source, whether natural (lightning) or anthropogenic. The numbers of anthropogenic vs. lightning wildfires in our data set varies as a function of ecoregion division, with the ratio ($N_{F \text{ anthropogenic}} / N_{F \text{ lightning}}$) = 0.2–0.8 in the seven Temperate and Tropical/Subtropical ecoregions (all divisions with codes > 300); 1.2–4.7 in Marine, Marine Mtns., Mediterranean Mtns., and Subtropical Mtns.; and 11–43 in the remaining seven ecoregion divisions.

Within each ecoregion division, we examine $\beta_{\text{anthropogenic}}$ and

model ecosystems (9–12, 25, 47, 49–53). Thus, variation in β between ecoregions may indicate differences in energy balance and rates of energy release in ecosystems according to differences in climate. An examination of β and its spatial and temporal relationships with the net primary production and the potential natural vegetation, in conjunction with more accurate estimates of energy released during combustion currently being developed (54), would contribute to understanding the role of wildfire in ecosystem energetics and the organization within open, dissipative systems (such as ecosystems) in general.

Recurrence Intervals of Wildfires. Using both α and β , we have calculated the recurrence intervals $T(\geq 0.01 \text{ km}^2)$ and $T(\geq 10 \text{ km}^2)$ for each ecoregion division (Table 1 and Fig. 3B). This type of mapping, and extensions of it, will prove very useful for government agencies and reinsurance groups when examining wildfire hazard.

Conclusions

Wildfires are costly in terms of damage and fatalities. The ways in which they begin and propagate are complex, with an indi-

vidual wildfire depending strongly on meteorological conditions, topography, vegetation, and, of course, wildfire-fighting efforts. Despite this complexity, the frequency–area of wildfires in conterminous U.S. ecoregions appear to robustly follow power-law (heavy-tailed) distributions, over more than five orders of burned area in each ecoregion. The simplicity of accepting power-law (or similar heavy-tailed) distributions, which exhibit scale-invariant behavior with excellent fits over many orders of magnitude, allows the use of the parameters β and α to describe the relative contribution and hazard of large wildfires within a wildfire regime. In turn, normalized β and α values allow for the explicit comparison and examination of wildfire-regime dynamics and change between ecoregions, as illustrated here.

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